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Exercise 3

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Problem 1. The plaintext hidden in the following ciphertext is part of a famous English play:

KPJDLCS PVHQWRK KCKRBKPJ DLCWILKR BGSKORKO VCVCNVEW OVQDLCIL YFIRRIGB
IVSXQKRB DLCSVCXX PKRAOWYX HMXIKKRG XLGCXGWI NVEWCQYX CNKVRC

(a) Determine the index of coincidence I_C . What can you derive from it¹?

Problem 2. The handling of long keys for Vernam ciphers is difficult. Therefore, autokey systems are proposed. For a given keyword $k = (k_0, \dots, k_{n-1})$ and message $m = (m_0, \dots, m_{l-1})$ the following two autokey systems are given.

$$c_i = \begin{cases} m_i + k_i \pmod{26} & 0 \leq i \leq n-1 \\ m_i + c_{i-n} \pmod{26} & n \leq i \leq l-1 \end{cases}$$

$$\hat{c}_i = \begin{cases} m_i + k_i \pmod{26} & 0 \leq i \leq n-1 \\ m_i + m_{i-n} \pmod{26} & n \leq i \leq l-1 \end{cases}$$

- Describe a ciphertext-only attack on $\mathbf{c} = (c_0, \dots, c_{l-1})$.
- Decrypt the cryptogram $\mathbf{c} = \text{DLGVTYOACOUVCEZA}$.
- Assume the keylength to be known. Describe a ciphertext-only attack on $\hat{\mathbf{c}} = (\hat{c}_0, \dots, \hat{c}_{l-1})$.
- Decrypt the cryptogram $\hat{\mathbf{c}} = \text{QEXYIRVESIUXXXKQVFLHKG}$ using keylength 2.

Problem 3. (*variance of the index of coincidence*) In Lemma 3.3 of the lecture notes, the expectation value of the index of coincidence was calculated for the ciphertext (C_1, \dots, C_n) with random variables C_1, \dots, C_n i.i.d.

- Derive the variance of the index of coincidence $\text{Var}(I_C)$ for the model of Lemma 3.3.

¹ $I_C \approx 0.0385$: polyalphabetic and uniformly distributed; $I_C \approx 0.0668$: monoalphabetic and English